

Q- At  $t=0$ , car A starts from rest at point 1. It moves towards the right with an acceleration of  $0.4t \text{ m/s}^2$ . At the same time car B starts from point 2 with a constant acceleration of  $2 \text{ m/s}^2$  to the right. Find:

- A) Speed of car 1 at the end of 200 m section.
- B) Time to travel of 200 meters by car A.
- C) Magnitude of car A's acceleration as it reached point 2.
- D) How far has car B moved when car A has reached point 2?
- E) Relative velocity and acceleration of car B with respect to car A when car A is at point 2.

A) & B) The acceleration of the car is not constant and hence we cannot use equations of motion.

The acceleration is the rate change of velocity and hence we can write

$$a = dv/dt = 0.4t$$

Integrating the equation gives us velocity as a function of time as

$$\int_0^v dv = \int_0^t 0.4t \, dt$$

$$\text{Or } v = 0.4(t^2/2) = 0.2 t^2 \quad \text{----- (1)}$$

Now as  $v$  is the rate of change of displacement, we can find the displacement as a function of time by integrating above equation 1

$$v = dx/dt = 0.2 t^2$$

$$\text{Or } \int_0^x dx = \int_0^t 0.2 t^2 \, dt$$

$$\text{Or } x = 0.2(t^3/3)$$

$$\text{Or } x = 0.0667t^3 \quad \text{----- (2)}$$

Time taken to reach 200 m is given by

$$200 = 0.0667t^3$$

$$\text{Or } t^3 = 3000.0$$

$$\text{Or } t = 14.38 \text{ s}$$

And velocity at this time is given by equation 1 as

$$v = 0.4 \cdot (t^2/2) = 0.2 t^2 = 0.2 (14.39)^2 = 41.38 \text{ m/s}$$

C) Acceleration at the time car 1 reaches 200 m is given by

$$a = 0.4 \cdot t = 0.4 \cdot 14.38 = 5.75 \text{ m/s}^2$$

D) Distance covered by car 2 when car 1 reaches point 2 (200 m) (constant acceleration)

$$[x_2 = u \cdot t + \frac{1}{2} a \cdot t^2]$$

or  $x_2 = 0 + 0.5 \cdot 2 \cdot (14.38)^2 = 206.78 \text{ m}$

E) Velocity of car B when A reaches point 2 is given by

$$v_B = u + a \cdot t = 0 + 2 \cdot 14.38 = 28.76 \text{ m/s}$$

Hence velocity of B relative to car A is given by

$$v_{BA} = v_B - v_A = 28.76 - 41.38 = -12.62 \text{ m/s}$$

Acceleration of car B relative to A is given by

$$a_{BA} = a_B - a_A = 2 - 5.75 = -3.75 \text{ m/s}^2.$$

(Negative sign shows the direction opposite to that of motion.)